# Slope effect on junction fire with two non-symmetric fire fronts 

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#### Abstract

Background. In Pedrógão Grande on 17 June 2017, two fire fronts merged and the propagation of the fire was influenced by the interaction of these non-symmetric fire fronts. Aims. This wildfire motivated us to study a junction fire with two non-symmetrical fire fronts. The analysis of the movement of the intersection point and the angle ( $\gamma$ ) between the bisector of the fire lines and the maximum rate of spread (ROS) direction is of particular relevance. Methods. The study was carried out at Forest Fire Laboratory of the University of Coimbra in Lousã (Portugal) with laboratory experiments. Key results. We found that, for small rotation angles ( $\delta$ ), the nondimensional ROS of the intersection point depends on the slope angle (a) and the initial angle between fire fronts. Conclusions. For high $a$, the non-dimensional ROS was highly influenced by the convection process and $\gamma$ where the maximum ROS occurred, increased when $\delta$ increased. However, the radiation process was more relevant for lower a and influenced the nondimensional ROS. For these cases, the maximum spread direction was close to that of the fire line bisector. Implications. The present work aimed to explain fire behaviour during the Pedrógão Grande wildfire.


Keywords: convergent fire fronts, dynamic fire behaviour, extreme fire behaviour, fire acceleration, fire behaviour, fire growth, fire modelling, forest fires, junction fires, merging fires.

## Introduction

Wildfire propagation is a complex and dynamic phenomenon that is not fully understood (Pastor et al. 2003; Sullivan 2009). Wildfire propagation depends not only on the classic triangle of 'fire factors' - topography, vegetation and meteorology - but also explicitly on time, given the dynamic interaction that it creates with the environment (Viegas 2004, 2006; Viegas et al. 2021, 2022).

The interaction of two different fire fronts during the merging of two fires (flank or spot fires) has been observed and studied by several authors in recent decades. During wildfires and prescribed fires, the interaction of the fire fronts or even some parts of the fires that merge between them cause a rapid spread of the fire and an increase in flame length (Brown and Davis 1973; Johansen 1984; Pyne 1984).

The merging of two fire-fronts that intersect at a small angle induces very high values of the rate of spread (ROS) and fire intensity of their intersection point, and follows a gradual velocity decrease in the course of time when the angle between fire fronts increases. This problem was studied by Viegas et al. (2012), who initially described this phenomenon as a 'jump fire', and developed a conceptual analytical model for the rate of advance of the intersection point or vertex of two oblique and symmetric fire fronts. Several research works on experimental, analytical and numerical simulation of this problem followed (Sharples et al. 2013; Viegas et al. 2013; Raposo et al. 2015, 2018; Hilton et al. 2016; Thomas et al. 2017; Sullivan et al. 2019; Filkov et al. 2021). The fire fronts were always symmetrical in relation to the vertex $V$ and there was no fuel bed to burn outside the linear straight fire lines. The results showed that the ROS of $V$ has a strong relationship with the initial angle between the merging fire fronts and the ROS increases suddenly from zero to values of the order of 100 times the basic ROS. A real fire
situation occurred in the merging of two large fires events: one of them near Canberra, Australia, on 18 January 2003 (Doogan 2006; Raposo 2016) and more recently in Pedrógão Grande, Portugal, on 17 June 2017 (Pinto et al. 2022).

The Pedrógão Grande wildfire was considered the worst wildfire in Portugal and Europe and motivated us to study the fire behaviour when two non-symmetric fire fronts converge.

## Physical problem

In the present study, it is assumed that the fire is produced by two straight lines $i_{1}$ and $i_{2}$, that intersect at point $A$ with an initial angle $\theta_{0}$ between them (Fig. 1) and spread in a uniform fuel bed layer on a flat surface $O X Y$, making a slope
(a)

(b)


Fig. I. (a) Schematic layout of the merging of two non-symmetric straight fire lines making an initial angle $\theta_{0}$ between them. The axis $O X$ is parallel to the slope gradient, the axis $O X_{1}$ represents the symmetry line of the fire configuration and the axis $O X_{m}$, defined by the green dashed line, represents the maximum ROS. (b) View of the Canyon Table DE4 of the Forest Fire Laboratory of the University of Coimbra.
angle $\alpha$ with the horizontal datum $O_{o} X_{o} Y_{o}$. The Cartesian coordinate system $O_{o} X_{o} Y_{o} Z_{o}$ is considered, in which $O_{o} Z_{o}$ is perpendicular to the ground. Point $A$ coincides initially with the origin of the reference Cartesian frame with axis $O X$ parallel to the slope gradient. The axis $O X_{1}$ represents the symmetry line of the junction fire and can be defined by the rotation angle $\delta$ that represents the angle between the line with the highest slope and the bisector of the fire lines. However, for each combination of $\alpha$ and $\delta$ angles, the maximum ROS occurs according to axis $O X_{m}$ and this axis is rotated at some angle $\gamma$, which represents the angle between the bisector of the fire lines and the maximum ROS. The fuel bed area is defined by $A B C$ and is covered by a uniform forest-type fuel layer able to support the spread of a surface fire. The merging of two linear fire fronts is illustrated schematically in Fig. $1 a$.

We consider two linear fire fronts defined by two straight lines $(A B$ and $A C$ ), non-symmetric in the $O X$ axis (Fig. 1a). Henceforward, the linear fire lines $A B$ and $A C$ are referred to as $i_{1}$ and $i_{2}$, respectively. In this study, it is assumed that at time $t_{i}=0 \mathrm{~s}$ and during the whole experiment there is no ambient wind velocity inside the laboratory and the fire lines are straight lines, simultaneously and instantaneously ignited.

## Material and methods

## Laboratory experiments

The experimental study was carried out at the Canyon Table DE4 (Fig. 1b) of the Forest Fire Laboratory of the University of Coimbra in Lousã (Portugal). The Canyon Table DE4 has a working area $6 \mathrm{~m} \times 8 \mathrm{~m}$, but only half of the area was used in the present laboratory experiments. The slope ( $\alpha$ ) of DE4 can be varied continuously in the range of $0-40^{\circ}$ using a hydraulic device. The fuel bed area was defined by a fixed angle between the fire fronts $\theta_{0}=30^{\circ}$ and a fixed length of 5.5 m , that is $8.73 \mathrm{~m}^{2}$. The selected value of $\theta_{0}=30^{\circ}$ was a compromise to perform our study. After an extensive test program using values of $\theta_{0}$ in the range of $10-90^{\circ}$, it was found that for smaller values of $\theta_{0}$ the test was very quick and it was difficult to measure the fire spread properties, while for large values of $\theta_{0}$ fire acceleration was not very important and the process that characterises the interaction between the two fire lines was not very relevant. This is consistent with previous work carried out on the subject of converging fronts by Viegas et al. $(2012,2013)$ and Raposo et al. (2018).

The fuel bed for the experiments was composed of dry particles of pine needles of Pinus pinaster with a constant load of $600 \mathrm{~g} \mathrm{~m}^{-2}$ (dry basis) (Viegas and Pita 2004; Xie et al. 2014; Raposo 2016; Raposo et al. 2018; Rodrigues et al. 2019; Viegas et al. 2021, 2022). During the preparation of each test, the air temperature $\left({ }^{\circ} \mathrm{C}\right.$ ), relative humidity (\%) and fuel moisture ( $m_{\mathrm{f}}$ ) were monitored and the conditions
of the fuel load and bulk density were controlled. The fuel bed height $\left(h_{f}\right)$ was aleatorily measured in five positions of the fuel bed, giving an average of 0.04 m . The approximate fuel properties follow: bulk density ( $\rho_{\mathrm{b}}$ ) of $14.50 \mathrm{~kg} \mathrm{~m}^{-3}$; fuel particle density $\left(\rho_{\mathrm{p}}\right)$ of $530 \mathrm{~kg} \mathrm{~m}^{-3}$; packing ratio $\left(\beta_{\mathrm{f}}\right)$, given by the ratio of $\rho_{\mathrm{b}}$ to $\rho_{\mathrm{p}}$, of 0.027 ; particle surface area to volume ratio $\left(\sigma_{f}\right)$ of $4100 \mathrm{~m}^{-1}$ and High Heat of Combustion of range $19.57-21.61 \mathrm{MJ} \mathrm{kg}^{-1}$ (Filipe dos Santos Viana et al. 2018). The fuel moisture content was measured twice with an A\&D ML50 moisture analyser for each test: before fuel bed preparation and before ignition. The time between fuel bed preparation and beginning of the burn test did not exceed 10 min , to guarantee that the moisture of the fuel bed in contact with ambient air did not change.

The basic ROS $R_{o}\left(\mathrm{~cm} \mathrm{~s}^{-1}\right)$ is a property of a given fuel bed when a linear fire front burns that fuel under no-slope and no-wind conditions and it depends principally on $m_{\mathrm{f}}$. For each series of tests performed, the value of $R_{o}$ was measured using a $1 \mathrm{~m} \times 1 \mathrm{~m}$ horizontal table with the same fuel bed properties - the corresponding values are given in Table 1.

The ignition of the two linear fire fronts ( $i_{1}$ and $i_{2}$ ) was performed by two persons to ensure that the lines started burning simultaneously, using two wool threads soaked in a mixture of petrol (50\%) and diesel fuel (50\%).

All tests were monitored and recorded in continuous mode with an infrared (IR) camera (FLIR SC660) and a video camera in the visible range, placed at the top of a lifting platform. In order to avoid parallax errors, the angles
between the IR camera optical axis and the ground surface of the Canyon Table DE4 were approximately $90^{\circ}$. The parameters considered for the IR camera were a temperature range of $300-1500^{\circ} \mathrm{C}$, an emissivity value of 0.98 (Dlugogorski et al. 2014) and an acquisition rate of 15 Hz . A threshold of $350^{\circ} \mathrm{C}$ was used to avoid obstruction of the view by the plume of the fire (Xie et al. 2014; Liu et al. 2015). The IR videos were used to obtain the fire contour perimeter with pre-defined times adjusted for each test in accordance with $\alpha$. More details about this methodology can be seen in Raposo (2016), Raposo et al. (2018) and Rodrigues et al. (2019).

In order to reduce uncertainty, three replication tests (T1, T2 and T3) were performed for each set of parameters (Table 1). For the symmetric condition ( $\delta=0^{\circ}$ ), we only performed one test and validated our results with previous work developed by Raposo (2016) and Raposo et al. (2018).

## Evaluation of the ROS

The evaluation of the merging process of the two fire lines showed a change of the angle $\theta$ between them. The angle between the fire lines increased during the burning of the fuel bed and tended to be close to $180^{\circ}$, which corresponds to a straight line. According to Raposo et al. (2018), the ROS $R_{A}$ near the intersection point of two fire lines (point $A$ ) has a functional dependence:

$$
\begin{equation*}
R_{A}=f\left(\theta_{0}, \alpha, \delta, m_{f}, \ldots, t\right) \tag{1}
\end{equation*}
$$

Table I. Parameters of the non-symmetric junction fires cases considered in the present study.

| Ref. | $a\left({ }^{\circ}\right)$ | $\delta\left({ }^{\circ}\right)$ | Designation |  |  | $m_{f}(\%)$ |  |  | $R_{\circ}\left(\mathrm{cm} \mathrm{~s}^{-1}\right)$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | TI | T2 | T3 | TI | T2 | T3 | TI | T2 | T3 |
| 1 | 10 | 0 | 1-JFOIO | - | - | 10.99 | - | - | 0.352 | - | - |
| 2 |  | 5 | I-JF510 | 2-JF510 | 3-JF510 | 13.89 | 10.99 | 12.32 | 0.228 | 0.328 | 0.290 |
| 3 |  | 10 | 1-JFIOIO | 2-JF1010 | 3-JFIOIO | 13.25 | 10.99 | 12.30 | 0.276 | 0.328 | 0.298 |
| 4 |  | 15 | I-JFI5IO | 2-JFI5IO | 3-JFI5IO | 13.25 | 10.99 | 11.01 | 0.226 | 0.328 | 0.310 |
| 5 | 20 | 0 | I-JFO20 | - | - | 13.90 | - | - | 0.235 | - | - |
| 6 |  | 5 | I-JF520 | 2-JF520 | 3-JF520 | 13.25 | 12.10 | 10.99 | 0.267 | 0.247 | 0.340 |
| 7 |  | 10 | 1-JF1020 | 2-JF1020 | 3-JFI020 | 13.25 | 13.28 | 13.51 | 0.221 | 0.221 | 0.221 |
| 8 |  | 15 | I-JFI520 | 2-JF1520 | 3-JFI520 | 13.25 | 12.15 | 11.99 | 0.289 | 0.241 | 0.265 |
| 9 | 30 | 0 | I-JF030 | - | - | 13.64 | - | - | 0.209 | - | - |
| 10 |  | 5 | I-JF530 | 2-JF530 | 3-JF530 | 14.03 | 14.29 | 10.99 | 0.247 | 0.221 | 0.340 |
| 11 |  | 10 | I-JFI030 | 2-JF1030 | 3-JFI030 | 12.49 | 14.29 | 11.50 | 0.245 | 0.218 | 0.294 |
| 12 |  | 15 | I-JFI530 | 2-JFI530 | 3-JFI530 | 12.49 | 13.90 | 11.50 | 0.245 | 0.203 | 0.294 |
| 13 | 40 | 0 | I-JFO40 | - | - | 11.86 | - | - | 0.255 | - | - |
| 14 |  | 5 | I-JF540 | 2-JF540 | 3-JF540 | 13.61 | 12.23 | 12.24 | 0.221 | 0.282 | 0.282 |
| 15 |  | 10 | I-JFI040 | 2-JF1040 | 3-JFI040 | 13.64 | 12.36 | 12.37 | 0.263 | 0.249 | 0.249 |
| 16 |  | 15 | I-JFI540 | 2-JF1540 | 3-JF1540 | 14.88 | 12.38 | 12.39 | 0.197 | 0.243 | 0.243 |

where dots represent the wide set of parameters required to define the fuel bed properties and $t$ is the time that each test lasted after ignition. We consider $t$ as an explicit variable because during the course of the time the fire behaviour changes as it is a dynamic process (Xavier Viegas 2004; Viegas et al. 2021, 2022).

However, the distance $x_{A}$ travelled by point $A$ and the time $t$ are not independent of each other and the distance $x_{A}$ at a given time $t$ is given as follows:

$$
\begin{equation*}
x_{A}=\int_{0}^{t} R_{A} \times \mathrm{d} t \tag{2}
\end{equation*}
$$

and Eqn 1 can be replaced:

$$
\begin{equation*}
R_{A}=f\left(\theta_{0}, \alpha, \delta, m_{\mathrm{f}}, \ldots, x\right) \tag{3}
\end{equation*}
$$

The role of $\theta_{0}$ has been studied extensively by several authors, showing that this is a relevant parameter in the development of junction fires (Viegas et al. 2012; Sharples et al. 2013; Thomas et al. 2015). In the present work, we consider for all experimental laboratory tests a constant value of $\theta_{0}=30^{\circ}$.

The $\alpha$ had the following values: $10^{\circ}, 20^{\circ}, 30^{\circ}$ and $40^{\circ}$. For each set of these parameters, the $\delta$ of linear fire fronts was $0^{\circ}, 5^{\circ}, 10^{\circ}$ and $15^{\circ}$ (Fig. 2). We assume that $\delta$ of linear fire fronts was of the same order of magnitude as the angles between the studied fire fronts $\theta_{0}=30^{\circ}$. We chose this angle because we wanted to identify the smallest angle that would initiate fire behaviour changes.

The $m_{\mathrm{f}}$ influenced the basic ROS $R_{o}$. The characteristic parameters of the fuel bed were $h_{\mathrm{f}}, \rho_{\mathrm{b}}$ and residence time $t_{o}$. These parameters for all experimental laboratory tests were in the same range of values. For further details about $t_{o}$ see Viegas (2006).


Fig. 2. Angle $\delta$ of linear fire fronts changes between $\delta=0^{\circ}$ and $\delta=15^{\circ}$. This figure shows (a) $\delta=0^{\circ}$ and (b) $\delta=10^{\circ}$.

The problem being analysed can be formulated as a function of either time or distance:

$$
\begin{equation*}
R_{A}=f_{1}\left(\alpha, \delta, R_{o}, t\right)=f_{2}\left(\alpha, \delta, R_{o}, x\right) \tag{4}
\end{equation*}
$$

The displacement velocity of the intersection point $A$ of the two fire lines was analysed over time from its original position $O$. The $\delta$ changed the symmetry of the boundary conditions of fire fronts in relation to the maximum slope angle and the intersection point. For each set of values of $\alpha$ and $\delta$, the maximum ROS was along the $O X_{m}$ axis. In order to compare the results with other fuel bed types - although the same type of fuel bed was always used in the present experimental program - and minimise the effect of $m_{\mathrm{f}}$ on $R_{A}$ in the tests performed under different conditions, we used non-dimensional ROS $\left(R_{A}^{\prime}\right)$ of the intersection point defined by the following:

$$
\begin{equation*}
R_{A}^{\prime}=\frac{R_{A}}{R_{o}} \tag{5}
\end{equation*}
$$

where $R_{o}$ represents the basic ROS ( $\mathrm{cm} \mathrm{s}^{-1}$ ) under no-slope and no-wind conditions.

## Statistical analysis

In order to reduce uncertainty, three replications (T1, T2 and T3) were performed for each set of parameters $\delta=5^{\circ}$, $10^{\circ}$ and $15^{\circ}$ (Table 1). The results presented are the average of three replications for each parameter set and error bars represent $\pm 95 \%$ confidence intervals.

We consider that the ROS of the intersection of point $A$ can be influenced by $\alpha$, which changes the flame geometry, the convection and radiation process, and by $\delta$ of the two fire lines in relation to the maximum slope. In order to check the combined influence of each variable, analysis of variance (ANOVA) was used to test for the effects of slope ( $\alpha=10^{\circ}, 20^{\circ}, 30^{\circ}$ and $40^{\circ}$ ) and the $\delta$ of linear fires fronts changes $\left(\delta=5^{\circ}, 10^{\circ}\right.$ and $15^{\circ}$ ). An ANOVA is a statistical method for determining the existence of differences among several population means, which requires the analysis of different forms of variance associated with the random samples under study, according to Devore (2010).

## Results and discussion

## ROS analysis

In order to analyse the role of $\alpha$ and $\delta$ of the fire fronts in relation to the maximum slope, a series of laboratory experiments were carried out (Table 1). Based on general observations of fire behaviour (in loco, IR and visible videos) during the experiments, there was a large change in fire dynamics behaviour when the slope increased in comparison to the effect of the small rotations $\delta$ tested in the presented work.

In order to assess these dynamic changes, in each test, we estimated the ROS $R_{A}$ for the intersection point $A$ of the two fire fronts. We used specific pre-defined times to obtain the fire perimeter plots with the IR camera according to the slope angle of each test: $\alpha=40^{\circ}$ and $30^{\circ}$ for $\Delta \mathrm{t}=2 \mathrm{~s}$, $\alpha=20^{\circ}$ for $\Delta \mathrm{t}=5 \mathrm{~s}$ and $\alpha=10^{\circ}$ for $\Delta \mathrm{t}=10 \mathrm{~s}$. The $R_{A}^{\prime}$ was calculated according to Eqn 5 and the basic ROS ( $R_{o}$ ) for each set of parameters is given in Table 1. The average, minimum, maximum and standard deviation (s.d.) values of $R^{\prime}{ }_{A}$ for three experiments (T1, T2 and T3) and for each $\delta\left(5^{\circ}\right.$, $10^{\circ}$ and $15^{\circ}$ ) were calculated (Table 2). In total, 40 experiments were performed specifically for this study and we also used 12 tests for symmetrical conditions performed earlier.

For each set of conditions tested, across all slope angles considered, the average $R^{\prime}{ }_{A}$ values ranged between 13.74 $\left(\alpha=10^{\circ}\right.$ and $\delta=5^{\circ}$ ) and $121.27\left(\alpha=40^{\circ}\right.$ and $\left.\delta=15^{\circ}\right)$. The average $R_{A}^{\prime}$ was generally largest when the slope or rotation angle increased (Table 2). Two-way ANOVA with replication indicated that the $R_{A}^{\prime}$ was significantly ( $P<0.05$ ) affected by $\alpha$, but the $\delta$ considered for the two fire fronts did not significantly $(P>0.05)$ affect $R^{\prime}{ }_{A}$. For further information about $P$-values please see Andrade (2019).

In order to analyse the influence of $\delta$ in the ROS of the intersection point $A$, we compared the values of $R^{\prime}{ }_{A}$ with the symmetrical boundary conditions ( $\delta=0^{\circ}$ ) previously developed by Raposo et al. (2018). However, for clarity, in the following figures, we represent the average results for the three repetitions run in the same conditions, with s.d. bar, representing $\pm 95 \%$ confidence intervals. The fire spread can be described as a function of either time or space (distance), in accordance with Eqn 4, and the behaviour of fire spread was non-monotonic (cf. Viegas et al. 2021, 2022).

The average $R_{A}^{\prime}$ values for each $\alpha$ and each $\delta$ were plotted as a function of time and displacement distance (Fig. 3). The $R_{A}^{\prime}$ values for $\delta=5^{\circ}, 10^{\circ}$ and $15^{\circ}$ were compared with the $R_{A}^{\prime}$ for the two symmetric fire fronts ( $\delta=0^{\circ}$ ). Despite the random nature of the fluctuations of $R^{\prime}{ }_{A}$ for each set of parameters used, there was a good relationship between the tests performed with $\delta\left(5^{\circ}, 10^{\circ}\right.$ and $15^{\circ}$ ) and symmetric boundary ( $\delta=0^{\circ}$ ) condition, and
the $R_{A}^{\prime}$ values tended to follow the same natural fluctuations for the time and distance travelled by point $A$.

The behaviour of the interaction of two linear fire lines is non-monotonic (Viegas et al. 2021, 2022) and the oscillations tend to increase with the slope angle because the convection process increases and dominates the interaction of these fire fronts. Junction fires are defined by two different phases: acceleration and deceleration phases. In the cases with lower slope angles (see Fig. 3 for $\alpha=10^{\circ}$ and $20^{\circ}$ ) the acceleration phase was very short, whereas the deceleration phase was more evident in these cases. For the lower $\alpha$, this was associated with the radiation process becoming more relevant compared to the convection process. The opposite occurred for the highest $\alpha$ (see Fig. 3 for $\alpha=30^{\circ}$ and $40^{\circ}$ ), for which the deceleration phase was not so evident and, in some experiments, the fire accelerated over the entire combustion table, possibly without reaching its maximum ROS value. The convection process was dominant for these $\alpha$ and the ROS of the intersection point $A$ developed very rapidly with the highest oscillations. The measurements were difficult to acquire because point $A$ displaced very rapidly and, in these cases, the standard deviation and the error bars tended to increase.

## Angle of the maximum ROS

In order to assess the overall role of the parameters $\alpha$ and $\delta$, the angle $\gamma$ corresponding to the maximum ROS was measured for each set of parameters. The average values of $\gamma$ were plotted as a function of the angle between the bisector of the linear fire lines and the line with the highest slope with the $95 \%$ confidence intervals, for all tests performed (Fig. 4). For the higher value of the slope ( $\alpha=30^{\circ}$ and $40^{\circ}$ ), $\gamma$ had a similar trend and, in those cases, the axis, where the maximum ROS occurred, was influenced more by the convection process. However, for the lower values of slope ( $\alpha=10^{\circ}$ ), $\gamma$ tended to decrease and the maximum ROS was near the bisector of the fire lines $\left(\gamma \sim 1^{\circ}\right)$. In that case, the radiation process in the vicinity of point $A$ was more relevant than the convection process. The fitted lines were given by the linear relationship between $\gamma$ (the angle

Table 2. Summary of the non-dimensional $\operatorname{ROS}\left(R_{A}^{\prime}\right)$ for experiments at three $\delta$ rotation angles $\left(5^{\circ}, 10^{\circ}\right.$ and $\left.15^{\circ}\right)$.

| Ref. | $a\left({ }^{\circ}\right)$ | $\delta\left({ }^{\circ}\right)$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 5 | 10 | 15 |
| 1 | 10 | 13.74 (3.81-43.15, 1.10) | 14.19 (3.41-51.43, 0.86) | 14.66 (2.58-46.47, 2.34) |
| 2 | 20 | 32.20 (6.14-80.89, 6.12) | 36.67 (1.48-93.35, 1.48) | 26.90 (5.47-81.18, 2.83) |
| 3 | 30 | $\begin{gathered} 75.44 \\ (25.2 \mathrm{I}-\mathrm{I} 36.26,12.17) \end{gathered}$ | $\begin{gathered} 8 \mathrm{I} .79 \\ (46.68-\mathrm{I} 82.80,7.8 \mathrm{I}) \end{gathered}$ | 77.27 (28.31-137.49, 7.69) |
| 4 | 40 | $\begin{gathered} 82.12 \\ (25.42-121.77,11.40) \end{gathered}$ | $\begin{gathered} 90.60 \\ (34.10-147.00,3.14) \end{gathered}$ | $\begin{gathered} 121.27 \\ (78.16-156.73,12.06) \end{gathered}$ |

Values in the table are composed by average (min-max, s.d.). A $R_{A}^{\prime}$ of $I 0$, for example, equates to experiments with 10 times the basic ROS ( $R_{0}$ : ROS no wind and no slope).


Fig. 3. Evolution of the non-dimensional $\operatorname{ROS}\left(R_{A}^{\prime}\right)$ as a function of the time and distance for different slope angles (a) and different rotation ( $\delta$ ) of the fire fronts. The average $R_{A}^{\prime}$ values of the three replications with $95 \%$ confidence intervals ( $\delta=5^{\circ}, 10^{\circ}$ and $15^{\circ}$ ) were plotted with the symmetrical boundary conditions ( $\delta=0^{\circ}$ ): (a) $a=10^{\circ}$, (b) $a=20^{\circ}$, (c) $a=30^{\circ}$ and (d) $a=40^{\circ}$.


Fig. 4. The angle between the bisector of the fire lines and the maximum ROS $(\gamma)$ as a function of the angle between the bisector of the fire lines and the line with the highest slope ( $\delta$ ). The average $\gamma$ values are plotted with the $95 \%$ confidence intervals for each case. The dashed lines represent the fitted linear regressions of the data values for each slope angle (a).

Table 3. Coefficients $k_{1}$ and determination coefficients $\left(R^{2}\right)$ for the fitted linear regressions of the data values for each slope angle (a) presented in Fig. 4.

| Ref. | $a\left({ }^{\circ}\right)$ | $k_{1}$ | $R^{2}$ |
| :--- | :---: | :---: | :---: |
| 1 | 10 | 0.067 | 0.917 |
| 2 | 20 | 0.257 | 0.999 |
| 3 | 30 | 0.425 | 0.998 |
| 4 | 40 | 0.429 | 0.993 |

between the bisector of the fire lines and the maximum ROS) and $\delta$ (the angle between the bisector of the linear fire lines and the line with the highest slope), and can be expressed as follows:

$$
\begin{equation*}
\gamma=k_{1} \delta \tag{5}
\end{equation*}
$$

where $k_{1}$ is the slope of each fitted line. For each case, we obtained the respective values of $k_{1}$ and the determination coefficients ( $R^{2}$ ) of the linear regression (Table 3).

Two-way ANOVA with replication for all data values of the angle between the bisector of the fire lines and the maximum $\operatorname{ROS}(\gamma)$ indicated that $\gamma$ was significantly affected ( $P<0.05$ ) by the $\alpha$ and $\delta$ considered for the two fire fronts.

## Conclusion

Analysis of the junction fires with non-symmetric linear fire lines based on laboratory-scale experiments was performed for different inclined fuel beds ( $\alpha=10^{\circ}, 20^{\circ}, 30^{\circ}$ and $40^{\circ}$ ) and different sets of rotation conditions of fire fronts
( $\delta=0^{\circ}, 5^{\circ}, 10^{\circ}$ and $15^{\circ}$ ). The evolution of the fire front consisted mainly of the advance of the intersection point $A$, with an initial angle $\theta_{0}=30^{\circ}$ between fire lines. For the $\delta$ tested, the random fluctuations of the non-dimensional ROS $R_{A}^{\prime}$ had a good relation between the test performed with $\delta\left(5^{\circ}, 10^{\circ}\right.$ and $\left.15^{\circ}\right)$ and symmetric boundary condition ( $\delta=0^{\circ}$ ), during the time and distance travelled by point $A$. For $\alpha=10^{\circ}$ and $20^{\circ}, R^{\prime}{ }_{A}$ was quite similar to the symmetric condition $\delta=0^{\circ}$. With these laboratory tests, we conclude that $R^{\prime}{ }_{A}$ of the intersection point $A$ for small $\delta$ depended on $\alpha$, but $\delta$ did not influence $R^{\prime}{ }_{A}$. However, for higher $\alpha$, the convection process was dominant and changed $\gamma$ where the maximum ROS occurred; for the lower $\alpha$, the variation of $\gamma$ was lower and very close to $0^{\circ}$.

In future work, we intend to analyse in more detail the dynamic evolution of the fire and its interaction with the surrounding flow between the linear fire fronts. To better compare with wildfire situations, it is also important to increase the scale factor of the dimension of the linear fire length.

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